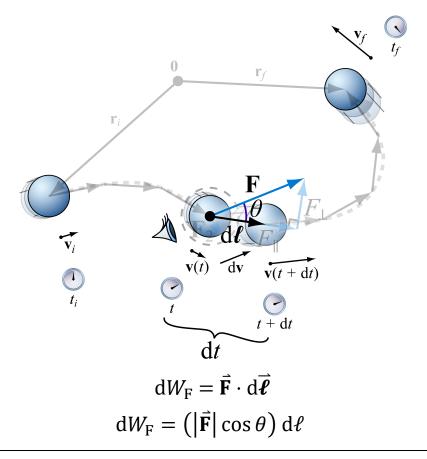
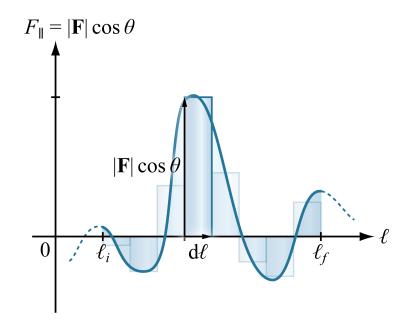
## Work performed along a path



## Steps for calculating work done along paths

- 1. Draw a large figure of the path.
- 2. Draw and label a representative differential displacement  $d\vec{\ell}$ .
- 3. Draw and label a force vector  $\vec{\mathbf{F}}$  applied at the tail of  $d\vec{\ell}$ .
- 4. Draw angle  $\theta$  between  $\vec{\mathbf{F}}$  and  $d\vec{\boldsymbol{\ell}}$ .
- 5. Obtain an expression for  $\vec{\mathbf{F}}$ .
- 6. Obtain an expression for  $d\vec{\ell}$ .
- 7. Calculate  $\vec{\mathbf{F}} \cdot d\vec{\boldsymbol{\ell}}$ .
- 8. Integrate the resulting expression.



$$\Delta W_{\mathrm{F}} = \int_{\vec{\mathbf{r}} = \vec{\mathbf{r}}_{i}}^{\vec{\mathbf{r}} = \vec{\mathbf{r}}_{f}} (|\vec{\mathbf{F}}| \cos \theta) \, \mathrm{d}\ell$$

$$\Delta W_{\mathrm{F}} = \int_{\vec{\mathbf{r}} = \vec{\mathbf{r}}_{i}}^{\vec{\mathbf{r}} = \vec{\mathbf{r}}_{f}} \vec{\mathbf{F}} \cdot \mathrm{d}\vec{\boldsymbol{\ell}}$$